VERSAT – P3D
Version 2006

QUASI-3D DYNAMIC FINITE ELEMENT ANALYSIS OF SINGLE PILES AND PILE GROUPS

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1.0 TECHNICAL MANUAL FOR VERSAT-P3D

1.1 Introduction

In addition to the quasi-3D theory background as described in Wu and Finn (1997a, 1997b), a special 8-node (4-beam) pile element has been used in VERSAT-P3D. In addition to representing the pile by a line-beam element, which does not take a physical space in a 3D model, each pile segment can also be represented by four beams arranged at the four corners of a pile cross-section. For simplicity, a pile cross-section, either square or circular, is modeled as a square. The four beams are rigidly tied to each other so as to produce identical response, or to act as a single pile element. The 4-beam pile element is introduced to take into account the effect of the physical space of a pile section on the response of a single pile or a pile group.

A VERSAT-P3D analysis can be carried out in one of the following three modes of analysis:

- **Impedance Mode**: Calculating dynamic stiffness and damping (impedance) in a frequency domain analysis;
- **Loading Mode**: Applying cyclic loads (shear forces and bending moments) at the pile head or at the pile cap in a frequency domain analysis; and
- **Shaking Mode**: Applying earthquake loads or dynamic loads at the pile head or at the pile cap in a time domain analysis.

The technical manual presents the theory and assumptions used in each of the above three modes of analyses.

---


1.2 Dynamic Stiffness and Damping of Pile Foundation

Under the Impedance Mode, dynamic stiffness and damping of pile foundations are obtained for the following:

- Horizontal Y direction
- Rotation about X axis (or in YoZ plane)
- Coupling term of above two, and
- Vertical Z direction

A separate model and thus a separate analysis will be required in order to compute horizontal and rotational stiffness and damping in the other horizontal direction, i.e., X direction. On the other hand, stiffness and damping for rotation about Z axis (or torsion) is not computed at present. If required, they need to be estimated from horizontal stiffness and damping.

1.2.1 Stiffness and Damping in Horizontal Direction

Subject to shear waves propagating in the vertical direction, the soils undergo mainly shearing deformations in the horizontal (XoY) plane except in areas near the piles where compression deformations develop in the direction of motion (Figure 1). The compressive deformations also generate shearing deformations in YoZ plane. In the light of these observations, assumptions are made that the dynamic motions are governed by shear waves in the XoY and YoZ planes, and compression waves in the Y direction. Deformations in the vertical direction and normal to the direction of motion are neglected to simplify a full 3D analysis to a quasi 3D analysis. The quasi 3D analysis considers displacements in one direction, Y, in a full 3D geometry.
As presented in Wu (1994), the governing equation describing the free vibration of the soil continuum in the Y direction is written as

\[ \rho_s \frac{\partial^2 \nu}{\partial t^2} = G^* \frac{\partial^2 \nu}{\partial x^2} + \theta G^* \frac{\partial^2 \nu}{\partial y^2} + G^* \frac{\partial^2 \nu}{\partial z^2} \]

Where \( \nu \) is displacement in the Y direction, \( \rho_s \) is the mass density of soil, and \( G^* \) is a complex shear modulus. The complex shear modulus \( G^* \) is expressed as \( G^* = G (1+i \cdot 2 \lambda) \) in which \( G \) is the shear modulus of soil, and \( \lambda \) is the hysteretic damping ratio of the soil. The parameter \( \theta \) was derived to be \( \theta = 2/(1-\mu) \) assuming a plane strain condition in the Y direction (Wu and Finn, 1999), and \( \mu \) is Poisson's ratio of the soil.
Displacements in the Y direction are set to be free at the lateral boundaries of the finite element model. Therefore, a quasi-3D model can be created to simulate free-field response by not using any piles in it.

The impedances, $K_{ij}$, are defined as the complex amplitudes of harmonic forces (or moments) that have to be applied at the pile head in order to generate a harmonic motion with amplitude of unity in a specified direction. The horizontal, cross-coupling, and rotational impedances of a pile at its head, represented by $K_{vv}$, $K_{v\theta}$, and $K_{\theta\theta}$, respectively, are defined as (Figure 2):

- $K_{vv}$ - with rotation fixed, the shear force required to cause a unit horizontal displacement
- $K_{\theta\theta}$ - with horizontal displacement fixed, the bending moment required to cause a unit rotation at the pile head
- $K_{v\theta}$ – a cross-coupling term of the above two

The impedances ($K_{vv}$, $K_{v\theta}$, $K_{\theta\theta}$) are complex values, and they are expressed by the real and imaginary parts as

$$K_y = k_y + i\omega c_y \quad \text{or} \quad K_y = k_y + i c_y \omega$$

Where $k_{ij}$ = stiffness, $C_{ij}$ = damping, $c_{ij} = C_{ij}/\omega$ = damping constant (or coefficient) for equivalent viscous damping, and $\omega$ = the angular frequency of the applied loads.
The hysteretic damping of soils is included in the complex shear modulus in Eq. [1]. The radiation damping of a 3D geometry adopted in VERSAT-P3D consists of energy dissipating boundaries including the horizontal base and the four vertical side surfaces.

1.2.2 Radiation Damping at Boundaries

The shear force caused by a particle velocity at the boundary is computed by

\[ F = \text{shear modulus (G) } \times \text{ particle velocity } \div \text{ shear wave velocity (V_s) } \times \text{ area (dA)} \]

With \( G = \rho \cdot V_s^2 \), then

\[ F = (\rho \cdot V_s \cdot dA) \times \text{ particle velocity} \]

Therefore, the damping matrix for an area in shearing is written as

\[ c_s = \int_A \rho \cdot V_s \ dA \quad [3] \]

Similarly the damping matrix for an area in compression is expressed as

\[ c_p = \int_A \rho \cdot V_p \ dA \quad [4] \]

Where \( V_p \) and \( V_s \) are the wave velocity in compression and in shearing. In VERSAT-P3D, damping matrix is formed using the consistent formulation of above equations.

Under the shear wave in the Y direction, the horizontal base and the two vertical side surfaces parallel to Y are assumed to be shearing boundary and the damping at these surfaces is derived using Eq. [3]. The two vertical side surfaces parallel to X are assumed to be in compression and the damping is derived using Eq. [4].

The energy transmitting boundary is applied only when the frequency of the loads is equal to or greater than 3.14 rad/sec (or 0.5 Hz). Otherwise, static boundary conditions are applied.

1.2.3 Stiffness and Damping in Vertical Direction

Subject to compression waves propagating in the vertical direction, the soil medium mainly undergoes compressive deformations in the vertical direction, Z (Figure 3). In the two horizontal directions, shearing deformations are generated due to the internal friction of the
soil. Although compressions occur in the two horizontal directions, assumptions are made that the normal stresses in the two horizontal directions due to vertical excitation are small and can be neglected. Therefore the dynamic motions of the soil are governed by the compression wave in the vertical direction, Z, and the shear waves propagating in the two horizontal directions, X and Y.

Figure 3 Quasi-3D Finite Element Model in Vertical Z Direction

Analogous to the governing equation in the horizontal Y direction, the quasi-3D wave equation of soil in the vertical direction is given by

$$\rho_z \frac{\partial^2 w}{\partial t^2} = G_x \frac{\partial^2 w}{\partial x^2} + G_y \frac{\partial^2 w}{\partial y^2} + \theta_z G_z \frac{\partial^2 w}{\partial z^2}$$

Where w is the soil displacement in the Z vertical direction. The parameter $\theta_z$ is derived to be $\theta_z = 2(1 + \mu)$ based on equilibrium of the model in the vertical Z direction.

The vertical impedance of a pile at its head, represented by $K_{zz}$, is defined as

- $K_{zz}$ - Vertical force required at the pile head that induces a unit vertical displacement.
The hysteretic damping of soils is included in the complex shear modulus in Eq. [5]. The radiation damping of a 3D geometry adopted in VERSAT-P3D consists of energy dissipating boundaries including the horizontal base and the four vertical side surfaces.

Under compression waves in vertical Z direction, the four vertical side surfaces parallel to Z are assumed to be shearing boundary and the damping at these surfaces is derived using Eq. [3]. The horizontal base is assumed to be in compression and the damping is derived using Eq. [4].

Again, the energy transmitting boundary is applied only when the frequency of the loads is equal to or greater than 3.14 rad/sec (or 0.5 Hz). Otherwise, static boundary conditions are applied.

1.2.4 Stiffness and Damping of Pile Group in Rocking

The rocking impedance of a pile group is a measure of resistance to rotation of the pile cap due only to the resistance of each pile in the group to vertical displacements. The rocking impedance of a pile group, represented by $K_{rr}$, is quantified as summation of moments of the axial pile forces about the centre of rotation, Point O in Figure 4, induced by a unit rotation about Point O. This definition is quantitatively expressed as

$$ F_r = K_{rr} \cdot \sum F_i $$

Where $r_i$ are distances between Point O and an individual pile in the group, and $F_i$ are the amplitudes of axial forces at the pile heads.

The rocking impedance, stiffness and damping, is computed assuming that piles located on the right side of Point O (Figure 4) mirror the piles located on the left side of Point O. In other words, only the piles on the left side of Point O are used in calculation, and the computed rocking impedance is multiplied by two to derive the rocking impedance of the pile group. This simplification only applies to calculation of rocking impedance. The calculation of vertical impedance of a pile group uses all piles in a 3D model.
The radiation damping in the calculation of rocking impedance takes the same form as in the calculation of vertical impedance.

### 1.2.5 Stiffness and Damping of Pile Group in Translation & Rotation

#### Piles Fixed to the Pile Cap

For a pile group with piles fixed (rigidly connected) to the pile cap, the rotational impedance of the pile group consists of two distinct components, the rotational impedance of each individual pile and the rocking impedance of the pile group. In a VERSAT-P3D calculation, the two components are computed separately. The rotational impedances of individual piles in the group are computed using a quais-3D model in the horizontal Y direction, and group effect is taken into account. The rocking impedance of the pile group is computed using a quasi-3D model in the vertical Z direction, and group effect is also taken into account.

The rotational impedance of the pile group is a summation of the two components. For this condition, the horizontal displacement of the pile cap is coupled with rotation of the pile cap.
Piles Pinned to the Pile Cap

For a pile group with piles pinned to the pile cap, the rotational impedance of the pile group consists of only the rocking impedance of the pile group. Rotational impedance of individual piles does not provide resistance to rotation of the pile cap because the piles do not carry bending moment at the pile head. The bending moment of the pile cap is carried out by axial forces in the piles.

For this condition, the horizontal displacement of the pile cap is uncoupled with, or independent to, the rotation of the pile cap, and the horizontal impedance of the pile group is the so-called “apparent stiffness and damping” that represents the shear force required to cause unit displacements when the pile head is free to rotation.

1.3 Response of Pile Foundation to Cyclic Loads

Under the Loading Mode, cyclic loads can be applied only in the horizontal Y direction. Response to cyclic loads applied in the other horizontal X direction needs to be carried out in a separate analysis. Analysis of response to cyclic loads in the vertical loads is not available at present.

The steady-state response of pile foundation subject to cyclic loads (harmonic shear force and/or bending moment) can be obtained by solving the equations of motion in the frequency domain using the same method as for the calculation of impedance. However, unlike in the impedance calculation where the analysis is linear elastic, the response analysis can be done either in linear elastic or in nonlinear elastic.

For problems involving high magnitude of loads that can induce nonlinear response in soils, the response to the cyclic loads will have to be computed using a method of iteration to seek compatibility between magnitude of loads and stiffness of soils. In a given iteration, the analysis is conducted as linear elastic. In a subsequent iteration of analysis, the soil stiffness (or shear modulus to be specific) and damping are adjusted based on the level of shear strain induced in the previous iteration. The relationships between shear modulus, damping ratio and shear strain can be specified by the users.
Shear failure and tension failure in soils may also be simulated by providing appropriate values of Yield Strength and Tensile Strength to a soil unit. A very low shear modulus is assigned to a soil element when the soil element is determined to be failed.

For response analysis of a pile group subject to cyclic loads, the rocking impedance of the pile group is taken into account by adding the rocking impedance, calculated in a separate analysis using the method described in Section 1.2.4, to the rotational term of complex stiffness in the equations of motion. This method for consideration of rocking impedance is illustrated in Figure 5.

![Figure 5 Consideration of Rocking Impedance of A Pile Group Subject to Horizontal Loads or Shaking in Y Direction](image)

## 1.4 Response of Pile Foundation to Earthquake Loads

Under the **Shaking Mode**, earthquake motions are applied in the horizontal Y direction only. Response analysis of pile foundations subject to vertical ground motions is not formulated at present although analysis of a pile group under horizontal shaking would also involve calculation of rocking stiffness and damping. The calculation of rocking impedance of a pile group is performed separately in the vertical Z direction (see Section 1.2.4) and in parallel to the time history analysis of the pile group. Therefore the rocking stiffness and damping of a pile group is updated continuously with time in the time domain analysis that reflects the nonlinear behaviour of soils.
1.4.1 Equations of Motion in Horizontal Y Direction

The governing equation of motion, Eq. [1], for quasi-3D analysis in the horizontal Y direction, has been solved in the frequency domain for calculation of pile impedance and for response analysis of pile foundations subject to cyclic loads at the pile head or the pile cap.

For response analysis of pile foundations subject to earthquake loads in the horizontal Y direction, the governing equation of motion (Eq. [1]) will be solved in the time domain that can simulate the time-dependent nonlinear behaviour of soils under earthquake shaking.

In a time domain analysis, the dynamic equilibrium equations of a soil-pile quasi-3D model can be written in a matrix form as

\[ [M] \ddot{\{v\}} + [C] \dot{\{v\}} + [K] \{v\} = -[M] [I] \ddot{\{y\}}_0(t) \]

in which \( \ddot{\{y\}}_0(t) \) is the base accelerations, \( [I] \) is a unit column vector, and \( \ddot{\{v\}} \), \( \dot{\{v\}} \) and \( \{v\} \) are nodal accelerations, velocities and displacements, respectively, relative to the model base. \([M], [C] \) and \([K] \) are the mass, damping and stiffness matrices. Direct step-by-step integration using the Wilson-\( \theta \) method is used to solve the equations of motion in Eq. [7].

The non-linear hysteretic behaviour of the soil is modeled by using a variation of the equivalent linear method similar to that used in the computer program SHAKE (Schnabel et al., 1972). Additional features such as tension cut-off and yielding are also incorporated in the program to simulate the possible gapping between soil and pile near the soil surface and yielding in the near field.

1.4.2 Simulation of Soil Non-Linear Stress-Strain Response

An equivalent linear method is employed in the program to model the non-linear hysteretic behaviour of soil. The basic assumption of this method is that the hysteretic behaviour of soil can be approximated by a pair of secant shear moduli and viscous damping ratios which are compatible with the level of shear strain. Typical relationships between shear modulus, damping ratio and shear strain can be found in the literature such as Seed and Idriss (1970), and Seed et al. (1986). This method has been accepted and widely used in engineering practice, and it has been incorporated in the computer code SHAKE (Schnabel et al., 1972).
for 1-D ground motion analyses and in QUAD-4 (Idriss et al., 1973) for 2-D plane strain analyses.

When the equivalent linear method is applied to earthquake problems involving irregular amplitudes of shear strains with time, the current practice is to assign a constant effective shear strain to a soil element to represent the variation of shear strains with time. The effective shear strain is commonly taken as 65% of the maximum shear strain experienced by the soil element during the life of earthquake shaking, and it is used to determine constant effective G and λ of the soil element that are then used in the final iteration of analysis.

To approximate better the nonlinear behaviour of soil under strong shaking, compatibility between secant shear modulus, damping ratio and shear strain should be sought at a time interval within which the shear strain history can be suitably represented by a single value of shear strain. This ensures that the time histories of shear moduli and damping ratios in each soil element are followed during the analysis in contrast with the equivalent linear approach described earlier in which a single effective value is used to represent the entire time history.

In a practical VERSAT-P3D analysis, the shear moduli and damping ratios are updated at specified time intervals which balance accuracy and computational time. For the analyses conducted to date using this method, it was found to be sufficient to update the soil properties at every 0.5 to 1.0 sec based on the peak strain levels from the previous time interval.

1.4.3 Equivalent Viscous Damping

The hysteretic damping ratio λ of soil is included in the dynamic analysis by using equivalent viscous damping. A procedure for estimating viscous damping coefficients for each individual element proposed by Idriss et al. (1974) is employed. The main advantage of this procedure is that a different degree of damping can be applied in each finite element according to its shear strain level. The damping is essentially of the Rayleigh-type, which is both mass and stiffness dependent.
The damping matrix \([C]_{\text{elem}}\) for a soil element is given by

\[
[C]_{\text{elem}} = \lambda_{\text{elem}} \left( \frac{8}{5} \omega_1 \left[ M \right]_{\text{elem}} + \left[ K \right]_{\text{elem}} \frac{2}{5\omega_1} \right)
\]

Where \(\omega_1\) is the fundamental frequency of the pile-soil system and is applied to each element. The frequency \(\omega_1\) is obtained by solving an eigen-value problem of the system and is updated with time. The hysteretic damping ratio, \(\lambda_{\text{elem}}\), is prescribed as a function of element shear strain (Seed et al., 1986), and this is also time dependent.

The viscous damping as expressed in Eq. [8] provides a damping ratio of \(\lambda_{\text{elem}}\) at two frequencies, one at \(\omega_1\) and the other at four times \(\omega_1\). At other frequencies, the damping ratio could be either higher or lower than \(\lambda_{\text{elem}}\).

### 1.4.4 Consideration of Rocking Stiffness and Damping of Pile Group

The rocking stiffness and damping constant of the pile group is taken into account by adding them, calculated in a separate analysis using the method described in Section 1.2.3, to the rotational term of stiffness and damping constants in the equations of motion. This method for the consideration of rocking impedance is illustrated in Figure 5.
1.5 Finite Element Formulation

1.5.1 Eight-Node Soil Element

An 8-node brick element is used to model the soil (Wu, 1994; Wu and Finn, 1997a). At each soil node, nodal variables consist of displacement in one direction only, i.e., Y direction in a horizontal analysis mode and Z direction in a vertical analysis mode. This is an assumption made in the quasi 3D model, and it is recognized that a node in 3D should contain displacements in X, Y and Z directions.

1.5.2 Two-Node Pile Element

Horizontal Analysis Mode

In this analysis mode, only the bending motion in the plane of motion (YoZ plane) is considered. At each pile node, nodal variables consist of displacement in Y direction, and rotation in the YoZ plane.

Piles are modelled using the ordinary Eulerian beam theory. Two-node pile elements are used to model the bending behavior of piles subject to horizontal loads. The pile mass density, $\rho$, is used to form the diagonal mass matrix of a pile element. The bending stiffness of the two-node pile element is given by

$$
[K] = \frac{EI}{L^3} \begin{bmatrix}
12 & 6L & -12 & 6L \\
6L & 4L^2 & -6L & 2L^2 \\
-12 & -6L & 12 & -6L \\
6L & 2L^2 & -6L & 4L^2 \\
\end{bmatrix}
$$

Where

- $E$ = Young's modulus of the structural member (the pile);
- $I$ = the bending moment of inertia of the pile\(^c\);
- $L$ = length of the pile element.

\(^c\) For example, $I=1/12*bh^3$ is for a rectangular section with a width of $b$ and a height of $h$; and $I=1/64\pi^d^4$ (where $\pi=3.1416$) is for a circular section having a diameter of $d$. 
**Vertical Analysis Mode**

In the vertical analysis mode, variables of a pile node contain only displacement in the vertical $Z$ direction. The axial stiffness of the two-node pile element is given by

$$K_A = \frac{EA}{L}$$

Where:

- $A = \text{sectional area of the pile}$ (E, L are the same as in Eq. [9]).

### 1.5.3 Eight-Node (4-Beam) Pile Element

In short, the 8-node pile element takes the space as it is an 8-node soil element and it has the properties of a 2-node beam element distributed into the eight pile nodes. In other words, a pile segment is represented by four beams arranged at the four corners of the 8-node pile element that represents the actual volume of the pile segment.

The purpose for using the 8-node pile element is to take into account the effect of pile diameter on pile response. A 2-node pile element is a line-beam element that does not take any physical space in a 3D model and therefore does not reflect the diameter effect on pile behaviour. The use of one or multiple 8-node pile elements to represent a large-diameter structure (such as a caisson, a vertical tunnel, or a shaft) section makes it possible to account for the diameter effect on response.

When a structure section is represented by multiple 8-node pile elements, the geometric properties (bending moment of inertia and section area) are evenly distributed to the number of elements on the section. Of course, if one 8-node pile element is used, the actual properties of the pile section are assigned to this pile element.

The procedure for such a representation has been verified by analyzing a vertical caisson itself without any soil elements surrounding it. It is strongly recommended that the behaviour of such a structural section of multiple 8-node elements be tested thoroughly prior to applying it to a soil-structure interaction analysis.
1.5.4 Batter Piles

Batter piles are approximately represented by modifying the horizontal stiffness of piles in a horizontal analysis, and the vertical stiffness of piles in a vertical analysis mode.

The horizontal stiffness of a pile element in Eq. [9] is modified as

\[ K_{\text{hor}} = \frac{12EI}{L_a^3} \cos^2 \alpha + \frac{EA}{L_a} \sin^2 \alpha \]

Where \( \alpha \) = the inclination angle to Z axis of the pile projected in YoZ plane, and

The vertical stiffness of a pile element in Eq. [10] is modified as

\[ K_{\text{vert}} = \frac{12EI}{L_a^3} \sin^2 \beta + \frac{EA}{L_a} \cos^2 \beta \]

Where \( \beta \) = the inclination angle of the pile to Z axis.

The calculation of pile stiffness is taken care of by the program once the angles of inclination, \( \alpha \) and \( \beta \), are entered for a pile.

The accuracy of the representation for batter piles is limited to the assumptions made above in association with the angle of pile inclination. It is recommended that the approximation be used for piles with batter angle less than 30°.
2.0 USERS MANUAL FOR VERSAT-P3D

2.1 Input and Output Data Files

2.1.1 For VERSAT-P3D Run

The Windows-based interactive program, VERSAT-P3D Processor, is used to prepare and save the input data file for the computing program, VERSAT-P3D Run. Depending on the problem at hand, one to two input data files are required:

- PILE3D.P3D: Main input file required by all analyses. When the Shaking Mode is run, the earthquake accelerations are appended at the end of this file manually;
- PILE3D.ATT: This file is required in a nonlinear analysis. It contains data describing nonlinear relationships between shear modulus, material damping, and shear strains. Some published data are compiled and included in this that is distributed.

The results of the analysis are contained in three output data files:

- PILE3D.OU1 This file contains echo of model data and computed stiffness and damping values.
- PILE3D.OU2 This file contains printed node and element response. Under Loading Mode, the response is in complex value and contains real and imaginary parts. Under Shaking Mode, the response is in real value.
- PILE3D.HIS This file contains time-history response of the finite nodes and elements that are requested by the users. The data can be retrieved using a support program, V-HIS3D.exe.

VERSAT-P3D always uses the above names as data files for input and output.

2.1.2 Terminology in VERSAT-P3D Processor and PILE3D.P3D

<table>
<thead>
<tr>
<th>Title</th>
<th>Description</th>
</tr>
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<tr>
<td>TITLE</td>
<td>Title of the problem</td>
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<tr>
<td>IMODE:</td>
<td>Analysis mode including one of the three modes:</td>
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<tr>
<td></td>
<td>Impedance Mode: impedance calculation (frequency domain analysis);</td>
</tr>
<tr>
<td></td>
<td>Loading Mode: harmonic loads at pile top/cap (frequency domain analysis); and</td>
</tr>
<tr>
<td></td>
<td>Shaking Mode: earthquake loads or loads at pile top/cap (time domain analysis).</td>
</tr>
<tr>
<td>KIMP</td>
<td>Index for computing impedance with a value of Yes or No</td>
</tr>
<tr>
<td>ICHANG</td>
<td>Method of analysis (linear elastic or nonlinear or equivalent linear)</td>
</tr>
<tr>
<td>IROCK</td>
<td>Pile head/cap condition using one of the three conditions:</td>
</tr>
<tr>
<td></td>
<td>piles are pinned to the cap and moments at pile heads=0;</td>
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<tr>
<td></td>
<td>piles are fixed to the cap; and</td>
</tr>
<tr>
<td></td>
<td>piles are fixed to the cap and rotation of the cap is zero.</td>
</tr>
</tbody>
</table>
ISYM  Index for mesh symmetry (a full size mesh; or a half size mesh)
ACCEG  Acceleration due to gravity such as 9.81 m/s² or 32.2 ft/s²
UNITWW  Unit weight of water such as 9.81 kN/m³ or 62.4 lb/ft³
PA  Atmospheric pressure such as 101.3 kPa or 2116 psf
NMAT  Total number of soil and pile material units
IMTYPG  Type of material; (5 for pile and 3 for soil)

For IMTYPG = 5:
- EMAT(I, 1) = Kₑ, Young's modulus constant (beam or truss), E=KₑPa
- EMAT(I, 2) = cross section area of the pile unit
- EMAT(I, 4) = bending moment of inertia of the pile unit
- EMAT(I, 5) = unit weight of the pile such as kN/m³
- EMAT(I, 6) = reduction factor; 0.5 if a pile is located on the X-symmetric line (parallel to Y-axis) in a half-mesh analysis, 1.0 for all other cases.
- EMAT(I, 7) = α inclination angle of a battered pile in the YOZ plane
- EMAT(I, 8) = β inclination angle of a battered pile to the vertical Z axis
- EMAT(I, 9) = damping ratio of the pile unit in percentage
- Others are not used for a pile material.

For IMTYPG = 3:
- EMAT(I, 2) = K₉, shear modulus constant (G= K₉ *Pa)
- EMAT(I, 3) = unit weight of the soil unit
- EMAT(I, 4) = strain factor used in a nonlinear analysis (such as 1.0 for using peak strain from previous time interval).
- EMAT(I, 5) = tensile strength of soil unit
- EMAT(I, 6) = iᵗʰ set of curve in PILE3D.att for describing modulus reduction and damping variation with effective shear strain such as 1.0 for 1st curve, 3.0 for the 3rd
- EMAT(I, 7) = Possion’s ratio (required)
- EMAT(I, 8) = shear strength of the soil unit
- EMAT(I, 9) = initial damping ratio of the soil unit in percentage

NNODES  Total number of nodes in the 3D model
NE  Total number of elements in the 3D model
NODE0  The principal pile cap node
NFIX  Total number of pile nodes at the pile top/cap
NODFIX  List of numbers of all pile top/cap nodes constrained/slaved to NODE0.
XMAX  X-coordinate where the energy transmitting boundary applied
YMAX  Y-coordinate where the energy transmitting boundary applied
XSYM  X-coordinate where the X-symmetric line is located
YSYM  Y-coordinate where the Y-symmetric line is located
ZCAP  Z-coordinate where the pile cap nodes are located
ZMAX  same as ZCAP
ZROCK  same as ZCAP
ZSOIL  Z-coordinate of the soil or ground surface
SHEAR0  Shear force applied at NODE0 (see notes below)
MOM0   Moment applied at NODE0.

Notes:

- The above two parameters are required only if Loading Mode is specified. Use 50% of actual values if a half-mesh is used for the analysis. For analysis of a pile group, a rigid pile cap is automatically assumed to exist at top of piles. The pile cap is represented by a single nodal point, NODE0, which is the first pile node at the level of the cap. All the remaining pile-top nodes are slaved or constrained to NODE0. Rocking stiffness, AKROCK, for the pile group is calculated for rotation resistance about Y-symmetric line (parallel to X-axis) including piles located between Y=0.0 and Y=YSYM.

Table 1

<table>
<thead>
<tr>
<th>Mode</th>
<th>Parameters</th>
<th>Descriptions</th>
</tr>
</thead>
<tbody>
<tr>
<td>Impedance</td>
<td>N_OMEG</td>
<td>Number of frequencies for impedance calculation</td>
</tr>
<tr>
<td></td>
<td>OMEG_0</td>
<td>First angular frequency (rad/sec) for impedance calculation</td>
</tr>
<tr>
<td></td>
<td>D_OMEG</td>
<td>Incremental frequency for each subsequent calculation.</td>
</tr>
<tr>
<td>Loading Mode</td>
<td>N_OMEG</td>
<td>• When N_OMEG&gt;=5, total loads are equally divided into (N_OMEG-4) increments.</td>
</tr>
<tr>
<td></td>
<td></td>
<td>• When N_OMEG&lt;5, total loads are applied and iterated N_OMEG times.</td>
</tr>
<tr>
<td></td>
<td>OMEG_0</td>
<td>Angular frequency (rad/s) of the shear/moment loads. When impedance is</td>
</tr>
<tr>
<td></td>
<td></td>
<td>requested, N_OMEG sets of impedance are calculated at this frequency.</td>
</tr>
<tr>
<td></td>
<td>D_OMEG</td>
<td>Not used</td>
</tr>
<tr>
<td>Shaking</td>
<td>N_OMEG</td>
<td>Rocking stiffness and damping of a pile group are updated, and shear</td>
</tr>
<tr>
<td>Mode</td>
<td></td>
<td>moduli and damping ratios of all soil elements are saved, for a total of</td>
</tr>
<tr>
<td></td>
<td></td>
<td>N_OMEG times (i.e., at every NPRN2 steps of numeric integration).</td>
</tr>
<tr>
<td></td>
<td>OMEG_0</td>
<td>• When impedance calculation is requested, the saved soil data are used</td>
</tr>
<tr>
<td></td>
<td></td>
<td>for calculation of impedance after the dynamic time-history analysis is</td>
</tr>
<tr>
<td></td>
<td></td>
<td>completed. A total of N_OMEG sets of impedance are calculated at this</td>
</tr>
<tr>
<td></td>
<td></td>
<td>angular frequency, OMEG_0 (rad/s);</td>
</tr>
<tr>
<td></td>
<td>D_OMEG</td>
<td>• When impedance calculation is not requested, this parameter is used for</td>
</tr>
<tr>
<td></td>
<td></td>
<td>computing rocking impedance only.</td>
</tr>
<tr>
<td></td>
<td></td>
<td>Not used</td>
</tr>
</tbody>
</table>

_NPRN2=NPOINT/N_OMEG, and a minimum NPRN2 of 50 is set by the program._
The following section applies when **Shaking Mode** is used.

- **NLOD**: Index on where the acceleration is applied, i.e., at a node or base shaking
- **NODMAS**: Node number of node where concentrated mass and/or stiffness is attached
- **PMASS(1)**: Mass at the node and it must be divided by 2.0 in a half mesh analysis
- **PMASS(2)**: Mass moment of inertia at the node and it must be divided by 2.0 in a half mesh analysis
- **PMASS(4)**: concentrated rotational stiffness
- **PMASS(5)**: concentrated rotational damping
- **PMASS(6)**: concentrated horizontal stiffness
- **PMASS(7)**: concentrated horizontal damping
- **PMASS(8)**: concentrated cross-coupling stiffness (including ‘-’ sign)
- **PMASS(9)**: concentrated cross-coupling damping (including ‘+’ sign)

- **IOPEQ**: Index about the type of input motion (earthquake type or harmonic SINE type)
- **NNOUT**: Total number of elements plus nodes at which time-history response are output to PILE3D.HIS.
- **NPOUT(J)**: List of node number or element number at which time-history response is to be output in PILE3D.HIS. A positive number represents a node number, and a negative number for an element.
- **NPOINT**: Number of input acceleration or load points (a maximum of 20000 points).
- **DTIME**: Time increment for input acceleration or load time history
- **AMPL**: Amplitude of SINE input acceleration or load
- **FREQ**: Frequency in Hz (or 1/sec) of the SINE motion
- **EQTITL**: Title of earthquake or load time history
- **FAMPL**: Scaling factor for input accelerations or loads
- **FMT**: Data format of the input accelerations or loads such as (8F10.4, 8G10.0)
- **ACCE(J)**: List of input accelerations or load time histories using FMT
2.1.3 Input Explanations for PILE3D.ATT

This file is needed only if a nonlinear analysis is used. It contains variations of shear modulus ratio and damping ratio as a function of shear strain.

1. **NCURVE** (I8)
   NCURVE: number of sets of curves contained in this file
   (One set of curves contains both modulus reduction and damping curves)

2. **NMOD** (I8)
   NMOD: number of data points used for describing this set of curves

3. **GAMM(I)** (16F8.0)
   GAMM(i): list of shear strains (from small to large) in percentage

4. **FMOD(I)** (16F8.0)
   FMOD(i): list of ratios of shear modulus $G/G_{max}$ corresponding to GAMM(i)

5. **FDMP(I)** (16F8.0)
   FDMP(i): list of damping ratios (in percentage) corresponding to GAMM(i)

* Input card 2 to 5 must be repeated NCURVE times.
2.2 Prepare Input Data

2.2.1 Define 3D Grid in X-Y-Z and Soil Units in Z

- Go to “DEFINE” and select “3D Finite Element Grid in XoY and Z”.
- Input Pile Diameter in Step 1;
- Choose method for grade in Step 2.
  - Click “Standard Single Pile Grid” or “Single Pile Grid for HighFreq…” can give you a predefined grid in XoY plane for a given Pile Diameter.
  - Input the Z-coordinate at top of each layer by providing the thickness of each layer from bottom-up (note: the base is always set to Z=0 and Z increases bottom-up).
  - Input soil material number for each layer under “SoilUnit”
- Input the Z-coordinate of soil (ground) surface in Step 3. In some cases, the pile cap is located above the soil (ground) surface, and the highest Z-coor should be greater than the ground surface in these cases. The pile cap is always set to be at the highest Z-coor of the model.
- Click “Update Change” to refresh the changes
- Click “Accept Change” will exit from this window and save the changes

![Set 3D Finite Element Grids in XoY and Z](image-url)
2.2.2 Define Piles for Location-Length and Pile Units

- Go to “DEFINE” and select “Pile Length and Unit”
- By default, pile locations are set at nodes as shown in Figure 7.

Note: On the computer screen, the Processor does not show the 8-node pile elements, but rather show the piles as one would see in reality. For instance, only one pile location is shown for a single pile analysis. The 8-node pile elements will be created automatically by the Processor when the data is saved. The “Pile Diameter” specified in the previous window is used as the length of a square pile section. It is therefore noted that the spacing between a grid line and its adjacent pile should be at least greater than half of the diameter of the pile because the actual space of the pile will be inserted at the pile location.

Figure 7 Define three piles at X=16 on the X-Symmetric Line
Other two methods for defining pile locations can be activated by checking the “Pile Setting Method” under SETTING, as shown in Figure 8.

The other two methods do not require insertion of pile elements because

- When pile locations are set at element centre, the elements identified will become 8-node (or 4-Beam) pile elements. In this case, the 8-node pile elements may not be square, i.e., can be rectangular.
- When pile locations are set using 2-node (or 1-Beam) pile elements, the piles are presented by a line and do not have physical space in 3D model.

Once pile locations in plan are set, pile length and pile material unit of each individual pile will need to be defined in the same window as shown in Figure 7.

It is noted that the pile length is the distance from the pile cap, the maximum Z-coordinate of the model, to the pile tip. The pile length is greater than the embedment depth of the pile (the distance from the ground surface to the pile tip) when the pile cap is elevated above the ground surface.

It is further noted that, in a Half-mesh analysis, different pile material numbers are assigned to piles that are located on the X-Symmetric line and to piles that are not. This is because piles on the X-Symmetric line require to be assigned a Reduction Factor of 0.5 in pile properties, meaning the same pile is equally shared by the other half of the grid that is not included in the analysis.

This Reduction Factor of 0.5 does not apply to 8-node pile elements defined by the “Setting Piles at Element Centre” method because these 8-node pile elements are not shared by the other half of the grid, even in a Half-mesh analysis.
2.2.3 Define Properties of Pile and Soil Units

- Go to DEFINE and select “Pile and Soil Properties”
- For the example being illustrated, Unit 1 is assigned to the three piles on the X-Symmetric line and thus has a Reduction Factor of 0.5. Units 2 and 3 are assigned to the two soil units, the red and the blue zones shown on the vertical grids. Unit 4 is assigned to a Reduction Factor of 1.0 and other properties same as Unit 1, and it can be assigned to piles located not on the X-Symmetric line. Unit 4 is not used in this example.
- It is noted that the total unit weight should be assigned to piles and soils although they may be submerged.

![Figure 9 Assign Properties of Pile and Soil Units](image-url)
2.2.4 Define Control Parameters for Analysis

- Go to DEFINE and select “Control Parameters”. This window will define what analysis will be carried out and how it is carried out.
- Figure 10 shows parameters under the **Loading Mode**. A combination of cyclic shear and moment (shear force=200 kN and bending moments=500 kN.m) is applied at the pile cap in a *Half-mesh* analysis while the piles are fixed to the pile cap. Note that “Shear of 100 and Moments of 250” are entered in the window. The frequency of the cyclic loads is 1 Hz (6.28 rad/sec). The loads will be divided into 6 increments and applied incrementally in a nonlinear analysis. A total of 10 analyses will be performed with the last load increment being iterated 5 times.

![Figure 10 Define Parameters under Loading Mode]
2.2.5 Define Parameters for Shaking Mode

- In Figure 10, click Shaking Mode under “Analysis Mode”
- Go to DEFINE and select “Setup for Shaking Mode”
- In Figure 11, an acceleration record from the 1971 San Fernando Earthquake will be appended MANUALLY by the user at the end of PILE3D.P3D. The record is written in 8 columns with a comma separating two columns. The first 2000 acceleration points from the record will be used in the dynamic analysis. The time increment for the record is 0.02 sec, and the acceleration values will be multiplied by 9.81 to convert into the unit of m/s² for accelerations to be used in the analysis (assuming the original values are in g).
- Time-histories response at node 500 and element 200 will be saved under PILE3D.HIS.
- No external mass or stiffness is applied at the pile cap (all zero in entries).

![Figure 11 Define Parameters under Shaking Mode](image-url)
2.3 Start An Analysis

- Save the prepared data as PILE3D.P3D
- Re-load the saved data back. The Processor can then verify the size of the model being less than the maximum allowed size, and show the node and element information of the 3D model. Without a reloading, these data are not available.
- Run VERSAT-P3D Run.exe under either Windows or Dos environment. Make sure that PILE3D.P3D is under the same directory as VERSAT-P3D Run.exe.

2.4 Retrieve Time-History Response

A separate computer program, called V-his3d.exe, is used to retrieve the time-history from PILE3D.HIS, a binary file containing time-history response. Another input file to V-his3d.exe is PILE3D.IN.

An example of PILE3D.IN, containing only two lines, is as follows:

Line 1: 4, 0, 0,
Line 2: 1, 2, 3, 4,

Line 1:
NDATA Total number of time-histories is requested;
N1 0, always
N2 0, not used

Line 2:
List of codes representing the specific quantity (such as acceleration, displacement, bending moment, shear force, etc.). These codes for retrieving a time-history response at a node or in an element are printed at the end of the output file, PILE3D.OU2.

3.0 EXAMPLES OF VERSAT-P3D MODELS

The example models shown in Figure 12 include the following:

- a). Structural analysis of vertical caissons only
- b). Analysis of free field response using a 10-layer model
- c). Analysis of a 12-pile group (shown as 8-pile group in a half-mesh analysis) with an elevated pile cap
- d). Analysis of a large 44-pile group (shown as 24-pile in a half-mesh analysis)

Analyses of these models are tasks for the users to complete.
a). Structural analysis of vertical caissons only

b). Analysis of free field response using a 10-layer model

c). VERSAT-P3D Model for analysis of 12-pile group (shown as 8-pile group in a half-mesh analysis) with an elevated pile cap
d). VERSAT-P3D model for analysis of a large 44-pile group (shown as 24-pile in a half-mesh analysis)

Figure 12 Examples of VERSAT-P3D Models
4.0 REFERENCES


